

## **Ph.D.Thesis of Salahaddin University-Erbil academic staff Studied Abroad**

**Title of thesis:** M-Axial Algebras Related to 4-Transposition Groups

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**Period of Study:** from 26/09/2011 to 30/01/2015

**Summary(Abstract):**

The main result of this thesis concerns the classification of 3-generated M-axial algebras  $A$  such that every 2-generated subalgebra of  $A$  is a Sakuma algebra of type  $NX$ , where  $N \in \{2, 3, 4\}$  and  $X \in \{A, B, C\}$ . This goal requires the classification of all groups  $G$  which are quotients of the groups  $T^{(s_1, s_2, s_3)} = \langle x, y, z \mid x^2, y^2, z^2, (xy)^{s_1}, (xz)^{s_2}, (yz)^{s_3} \rangle$  for  $s_1, s_2, s_3 \in \{3, 4\}$  and the set of all conjugates of  $x, y$  and  $z$  satisfies the 4-transposition condition. We show that those groups are quotients of eight groups. We show which of these eight groups can be generated by Miyamoto involutions. This can be done by classifying all possible M-axial algebras for them. In addition, we discuss the embedding of Fisher spaces into a vector space over  $GF(2)$  in Chapter 3.

**Acknowledgment:** I would like to record my great appreciation for Salahaddin University-Erbil-Kurdistan (<http://international.su.edu.krd>), for giving me the permission leave and giving me full salary study permission for the whole period of the study abroad.